## Level

## c

 M

## The Key Elements to Mathematics Success

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The following reviewers contributed to this edition, and we gratefully thank them for all their suggestions for improvements and clarifications.

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The Key Elements to Mathematics Success Description of Teacher's Guide



SOLVE
SOLVE is a 5 -step problem-solving paradigm taught in the first lesson of The Key Elements to Mathematics Success and throughout the program. SOLVE is an acronym which gives students step-by-step strategies for finding the solutions to word problems. The ultimate goal of teaching SOLVE is to provide students with a problem-solving strategy that can be applied to any concept they will encounter in algebra. The steps are as follows:

Study the Problem
Underline the question.
Answer the question, "What is this problem asking me to find?" in your own words.

Organize the Facts
Identify the facts.
Eliminate the unnecessary facts.
List the necessary facts.
Line up a Plan
Choose an operation or operations.
Write in words what your plan of action will be.
Verify Your Plan with Action
Estimate your answer.
Carry out your plan.
Examine Your Results
Does your answer make sense? (Compare your answer to the question.) Is your answer reasonable? (Compare your answer to the estimate.)
Is your answer accurate? (Check your work.)
Write your answer in a complete sentence.

## Cooperative Pairs

Working in cooperative pairs is a vital part of The Key Elements to Mathematics Success. Cooperative learning allows students at various performance levels to work together, using a variety of learning activities, to improve their understanding. Communication about the learning process is an essential element of working in cooperative pairs. This dialogue enhances student learning and creates a sense of responsibility on the part of the students. Cooperative learning can be a catalyst in creating an atmosphere of achievement and a sense of accomplishment on the part of the students when the task is successfully completed.

Levels of Teacher Support
The lessons are carefully designed with opportunities for modeling, guided practice, and independent practice.

## Modeling:

Each lesson contains "modeling boxes" which list step by step instructions on how to model each concept. Modeling steps are provided for concrete, pictorial, and procedural steps of the lesson.

## Guided Practice:

Detailed instructions about how to structure guided practice are given in each lesson. Guided practice is led and closely monitored by the teacher. Students may work individually or in pairs during the guided practice.

## Independent Practice:

Independent practice is provided through practice problems and homework in each lesson. Independent practice is structured to take place in the lesson following modeling and guided practice sections. Teachers can use the independent practice as a tool for informal formative assessment.
Word Problem Closure
At the end of the lesson, the SOLVE problem introduced at the beginning of the lesson is revisited. The student completes the additional steps of SOLVE, applying the lesson concept in a problem-solving situation.

Closure
Closure is a crucial part of every lesson and provides the teacher an opportunity to evaluate if the lesson objectives have been met. Teachers use the essential questions to reinforce the concept from the lesson, help organize the learning, and bring the lesson to its conclusion. A quick discussion of the essential questions will allow the teacher to informally assess student understanding of the material.

## Homework

Homework is provided at the end of each lesson to give students ample opportunity to practice the lesson concept.

## Quizzes

The lesson quizzes consist of 10 multiple-choice questions. These 10 questions cover the material taught in the lesson. The quizzes can also be used as homework, class work, review for a test, or as warm-ups.

## Review Activities

Review activities are provided for many lessons. There are a variety of engaging activities including scavenger hunts, chain reactions, "I Have, Who Has", and Mystery Squares. The activities are designed to provide multiple practice opportunities for the students in puzzle and game formats. The review activities incorporate the essential elements of cooperative learning and communication about the concepts.

The Key Elements to Algebra Success and the English Language Learner (ELL)

- SOLVE - A step-by-step procedure to attack word problems, dissecting the English language by identifying key words needed to solve the problem, and mapping out a plan with pictures and phrases to ultimately arrive at a well thought out answer. Steps can be written in students' native language while they are still becoming familiar with the process of SOLVE and gradually transitioning into English only.
The steps of SOLVE have been modified slightly for use with ELL students. The modified steps provide additional support and involve verbal communication about the process, which is a vital link for the ELL student:
S - Underline the question. TPIAMTF (this problem is asking me to find) - THE $\qquad$ . The students cannot just restate the question if they are made to start a sentence with the. O-Circle the necessary facts. When writing out the necessary facts, be as brief as possible and teach the students abbreviations right away (\$, \#, lb, cm, pkg. etc.).
L - Choose an operation and discuss a plan out loud. - +, •, / number of nuts + number of bolts $=$ total
total - number of boxes $=$ answer
V - Estimate the answer out loud. Then use the set-up created in the L step to carry out the plan.
E - Choose your answer.
- Cooperative Pairs - Working, questioning, and communicating with others regarding mathematics at all stages of learning. Activities are done in an interactive setting, encouraging language development along with mathematical development. This includes the pairing of ELL students who speak the same language(s) with others who may be at varying stages of their English language development.
- Modeling with Manipulatives - Students participate in activities leading to the discovery of on-grade-level mathematical concepts. Through this process, they develop mathematical understanding while exploring ways of expressing their discoveries in English. Manipulative use is consistent throughout the program. The appearance of each manipulative, their meaning, as well as the language used to describe the actions of these manipulatives remain the same throughout.
- Word Walls - Updated through the use of KEMS lessons, new math vocabulary words (and their meaning/pictorial representation) are added for every new concept as they are discovered. The Word Wall is an interactive tool for all learners and provides an additional language resource for ELL students. Additionally an Operation Word Wall is created by each class and used for solving word problems throughout the year. As an added resource, words can be written in both English and the native language of the learner. Pictures/descriptions are also encouraged next to words wherever appropriate.
- Video Clips of Each Lesson - Available for use in class at www.NTNmath.com, the video clips can help overcome the significant classroom language barriers ELL students face. These video clips, though in English, show key vocabulary words as a way of familiarizing students with appropriate vocabulary used to build a concept.


## Planning for your Key Elements to Mathematics Success Class

Materials Needed: include materials needed for both the teacher and the students including items from the manipulative kit, activities to prepare for pairs on cardstock, and/or pages to copy for class.
Objective: (from teacher lesson notes)
Essential Question: (from teacher lesson notes)
Word Wall Words: (from teacher lesson notes)
Agenda: Consider the following when planning each component of the lesson.

| Activity | Time Frame | Notes/Details |
| :---: | :---: | :---: |
| Environment | N/A | - Groupings used today - seating arrangements needed? <br> - Word Wall updates for this lesson? <br> - Agenda, Objective \& Essential Questions posted? <br> - Needed technology set up? |
| Warm-up | $\overline{\text { minutes }}$ | - What are some great questions to ask during the warm-up? <br> - How does this warm up relate to the lesson? <br> - How can this be modified to fit within the 5 minute time frame? |
| Fact Masters | $\overline{\text { minutes }}$ | - How will math facts be practiced today? (Group led, DVD, CD, quiz) <br> - What time in the lesson will it be done? <br> - Choral Drill or Quiz today? |
| Lesson | minutes | - What is the goal for today's lesson? <br> - What materials are needed? <br> - Is there an activity from the activities section of my <br> TE that I will use to support this lesson? <br> - How does the flow of this lesson encourage student discovery of the concept being covered? What questions need to be asked to guide the discovery of today's concept? <br> - How does this lesson fit in with my district pacing guide? <br> - How will this concept be enhanced with the traditional textbook? <br> - How will I instruct partners to work? <br> - Pages being covered today... <br> - Complete SOLVE Problem <br> ASK: What is the question asking me to find? (beginning of class) <br> What are my facts? <br> What is my plan? What operation is needed? <br> Estimate an answer. <br> Work out the answer. <br> Check over work, choose answer. <br> - What graphic organizer/foldable will be made/referenced? <br> - If time permits... <br> - Will this section be used today? <br> - If so, how? <br> - How will I use the quiz for this lesson? |
| Closure | $\overline{\text { minutes }}$ | - Essential Questions <br> - Homework assigned |

## Notes:

## Planning for your Key Elements to Mathematics Success Class

Materials Needed:

Objective:
Essential Question:
Word Wall Words:
Agenda:

| Activity | Time <br> Frame |  |
| :---: | :---: | :---: |
| Environment | N/A |  |
| Warm-up | $\overline{\text { minutes }}$ |  |
| Fact Masters | $\overline{\text { minutes }}$ |  |
| Lesson | $\overline{\text { minutes }}$ |  |
| Closure | $\overline{\text { minutes }}$ |  |
|  |  |  |

Notes:

## Planning for your Key Elements to Mathematics Success Class

Materials Needed:

Objective:
Essential Question:
Word Wall Words:
Agenda:

| Activity | Time <br> Frame |  |
| :---: | :---: | :---: |
| Environment | N/A |  |
| Warm-up | $\overline{\text { minutes }}$ |  |
| Fact Masters | $\overline{\text { minutes }}$ |  |
| Lesson | $\overline{\text { minutes }}$ |  |
| Closure |  |  |

Notes:

Planning for your Key Elements to Mathematics Success Class
Materials Needed:

Objective:
Essential Question:
Word Wall Words:
Agenda:

| Activity | Time <br> Frame |  |
| :---: | :---: | :---: |
| Environment | N/A |  |
| Warm-up | $\overline{\text { minutes }}$ |  |
| Fact Masters | $\overline{\text { minutes }}$ |  |
| Lesson | $\overline{\text { minutes }}$ |  |
| Closure | $\overline{\text { minutes }}$ |  |
|  |  |  |

Notes:

## Materials List

## Lesson 1

Paper for foldable ( 3 sheets of different colors for each student)
Stapler
" S " poster from packet

## Lesson 2

Foldable from Lesson 1
" 0 " poster from packet
Index card with $\sqrt{ }$ and $x$ on both sides
(1 per student pair)

## Lesson 3

Foldable from Lesson 1
"L" poster from packet
Index cards

## Lesson 4

Foldable from Lesson 1
"V" poster from packet

## Lesson 5

Foldable from Lesson 1
"E" poster from packet

## Lesson 6

Beans (2 per student pair)

## Lesson 7

Beans (50 per student pair)
Colored pencils

## Lesson 8

Copies of T212 or T213 on quiz days
Copies of T210 (1 set of numbers per student)
Copies of T211 (1 per student pair) Scissors
Fact Masters Curtain
Colored pencils
Gridded index cards
Beans (81 per student pair)
2 cups for each pair
Paper clips
Hole punch
Masking tape
Phase 2 - T208, T209, T214, T215,
T216-T222 and T223

## Lesson 9

Beans (50 per student pair)
Colored pencils
Lesson 10
Copies of T288 or T289 on quiz days
Copies of "TI/I" (total items/items)
cards on T283-T286
Copies of T287 (1 per student pair)
Scissors
Fact Masters Curtain
Colored pencils
Beans (81 per student pair)
Masking tape
Gridded index cards
Hole punch
Paper clips
Phase 2 - T281, T282, T288, T289,
T290, T291, T292-T298, and T299

## Lesson 11

Beans (50 per student pair)
Colored pencils

## Lesson 12

Centimeter cubes (24 per student pair)
Colored pencils

## Lesson 13

Two-colored counters (12 per student pair)
Colored pencils

## Lesson 14

Colored pencils
Two-color counters (18 per student pair)

## Lesson 15

Beans (16 per student pair)
Colored pencils

## Lesson 16

Fraction strips - Kit 1 and Kit 2
Scissors
Overhead fraction strips
Plastic bag (1 per student)
Colored pencils

## Materials List

## Lesson 17

Fraction strips - Kit 1 and Kit 2
Overhead fraction kit
Colored pencils

## Lesson 18

Fraction strips - Kit 1 and Kit 2
Overhead fraction kit Beans (4 per student pair)

## Lesson 19

Toothpicks (2 per student pair)

## Lesson 20

Large unit cube
(1 per group of 4 students)
Small unit cubes
(100 per group of 4 students)

## Lesson 21

Centimeter cubes
(32 per student pair)
Colored pencils

## Lesson 22

Paper for foldable
Colored pencils
Sticky notes
Scissors

## Lesson 23

Painter's tape
Sticky notes
Foldable from Lesson 22
Lesson 24
Copy Master T685 (1 per six students)
Copy Master T690 (1 copy - cut apart
to pass out to students)
Painter's tape
Two-color counters (1 per student pair)
Overhead two-color counters (1 per
student pair)
Fraction Kits 1, 2 and 3 (1 per student
pair)
Overhead fraction strips
Foldable from Lesson 22

Leson 25
Toothpicks (10 per student pair)
Colored pencils
Paper for foldable

## Lesson 26

Toothpicks (10 per student pair)
Colored pencils
Foldable from Lesson 25
Lesson 27
Centimeter cubes (40 per student pair)

## Lesson 28

3-inch sticky notes (4 per student pair) Colored pencils

## Lesson 29

Transparency cut-outs of T838
Copy Master T838 (1 per student pair)
Scissors
Glue

## Lesson 30

Transparency of Copy Master T865
Copy Master T865 (1 per student pair)
Scissors
Glue
Colored pencils

## Appendix A

Copies of T902 or T903 on quiz days
Copies of T901 (each student needs 1
set of numbers)
Scissors
Fact Masters Curtain
Colored pencils
Gridded index cards
Beans (18 per student pair)
Cups (2 per student pair)
Hole punch
Paper clips
Masking tape
Phase 2 - T899, T900, T904, T905,
T906-T912, and T913

## Materials List

## Appendix B

Copies of T943 or T944 on quiz days
Copy of of "Minuend/Subtrahend" cards
on T939 - T942 for teacher (Cut apart
for distribution to partners.)
Scissors
Fact Masters Curtain
Colored pencils
Beans (18 per student pair)
Masking tape
Gridded index cards
Hole punch
Paper clips
Phase 2 - T937, T938, T945, T946,
T947-T953, and T954

## Word Wall List

## Lesson 1

S - Study the Problem

## Lesson 2

O - Organize the Facts

## Lesson 3

L - Line up a Plan
addition
subtraction
multiplication
division
equals
together
add
plus
increase
sum
and
total
rises
grow
above
all together
altogether
"How many"
take away
difference
left over
minus
below
decrease
subtract
How much more?"
times
product
each
per
double
triple
of

Lesson 3 (cont.)
groups
multiplied
items
quotient
per equal groups
cut into
split
divide
is
same
equivalent
is equal to
Lesson 4
V - Verify Your Plan with Action
Lesson 5
E - Examine Your Results
Lesson 6
round
place value
ones
tens
hundreds
digit
scale

## Lesson 7

add
subtract
algorithm
addend
sum
minuend
subtrahend
difference
regroup
groups
items
inverse

## Word Wall List

## Lesson 8

groups
items
array

## Lesson 9

groups
items
array
multiply
product
factor

## Lesson 10

groups
items
dividend
divisor
quotient
total items
Lesson 11
groups
total items
items
division
quotient
dividend
divisor

## Lesson 12

unknown value
array
multiply
divide
equation
multiplication
division
fact family
Lesson 13
equation
unknown number
division
multiplication
groups
items
total items

## Lesson 14

equation
unknown value
equal sign
Lesson 15
pattern
sum
addend
product
factor
odd
even

## Lesson 16

numerator
denominator
fractions
halves
fourths
eighths
thirds
sixths
equivalent
legal trade
whole unit
Lesson 17
fraction
numerator
denominator
number line
whole unit
interval

## Word Wall List

## Lesson 18

equivalent fractions
number line
less than (<)
greater than (>)
equal (=)
Lesson 19
clock
minute
interval
analog clock
digital clock
Lesson 20
gram
kilogram
milliliter
liter
mass
volume

## Lesson 21

equation
unknown value
division
multiplication
groups
items
total items
Lesson 22
scale
picture graph
scaled picture graph
Lesson 23
scale
bar graph
scaled bar graph
$x$-axis
$y$-axis

## Lesson 24

line plot
$x$-axis
$y$-axis
Lesson 25
perimeter
formula
units
length
width
side

## Lesson 26

area
formula
square units
length
width
side

## Lesson 27

area
perimeter
dimensions

## Lesson 28

complex figure
area
non-overlapping

## Lesson 29

quadrilateral
attributes
congruent
right angles
parallel sides
rectangle
square
parallelogram
rhombus
trapezoid

## Word Wall List

## Lesson 30

unit fraction
area

## Appendix A

addend
sum
Appendix B
minuend
subtrahend
difference

