

The Key Elements to Mathematics Success

Teacher's Edition

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Table of Contents

Lessons

Teacher Note: When student pairs are using manipulatives to model concepts, they will need to use both partner books. Many times students need the concrete model to answer questions or bridge to the pictorial model on the following page.

	Lesson	Pages	Manipulatives	Word Wall Words	Foldable
1	SOLVE - S and O	Teacher Pages T1 – T19 Student Pages S1 – S7	Paper for foldable (3 sheets – different colors) Stapler "S" and "O" Posters Index cards ("N" and "U")	S – Study the Problem O – Organizer the Facts	- Oldable
2	SOLVE - L	, ,		L – Line up a Plan addition, subtraction, multiplication, division, equals, together, add, plus, and, incline, increase,	
		Student Pages S8 – S18		deposit, sum, total, rises, grows, above, take away, difference, decline, minus, withdraw, write a check, subtract, fewer, decrease, left over, "How many?" "How much more?" below, all together, times, product, each, of, groups, items, per, double, triple, multiplied, quotient, per equal groups, cut into, divvy, split, is, same, balanced, equivalent, divide, is equal to	SOLVE Foldable
3	SOLVE - V and E	Teacher Pages T40 – T59	Foldable from Lesson 1 "V" and "E" posters	V – Verify Your Plan with Action E – Examine Your Results	
		Student Pages S19 – S29			
		Ratios	and Proportional Rela	tionships	
4	Ratios and Unit Rates		Two-color counters (12 per student	ratio, quantity, compare, relationship, unit rate	
		Student Pages S30 – S39	pair) Toothpicks (9 per student pair)		
		Activity Page T877 Scavenger Hunt			
5	Ratios and Tables	5	(8 per student pair)	ratio, unit rate, coordinate plane, x-axis, y-axis, scale,	
				ordered pair, variable	
		Activity Pages T878 – T881 Scavenger Hunt			

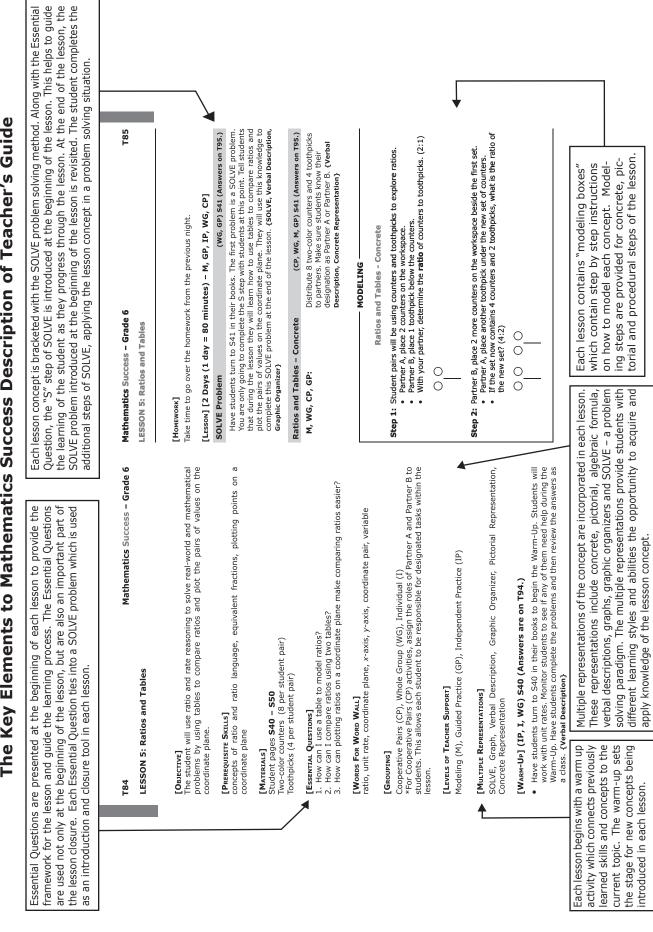
6	Unit Rate Problems	Teacher Pages T108 – T127 Student Pages S51 – S60 Activity Page T882 Chain Reaction	Index cards (5 per student pair) Toothpicks (5 per student pair) Two-color counters (10 per student pair) Painter's tape (4 small pieces per student pair)	ratio, tape diagram, constant rate, unit pricing, unit rate, variable
7	Percent as a Rate per	Teacher Pages T128 – T146	Centimeter cubes (70 per student r	ratio, percent, $\frac{\text{part}}{\text{whole}} = \frac{\%}{100}$
	100	Student Pages S61 – S69	pair) Colored pencils	whole roo
		Activity Page T883 Chain Reaction		
8	Converting Measurement	Teacher Pages T147 – T178	Calculators (optional)	ratios, identity property of multiplication, conversion
	with Ratios	Student Pages S70 – S84	f	factor, convert
		Activity Page T884 Chain Reaction		
		-	The Number System	1
9	Concept of Fractions	Teacher Pages T179 – T203	Fraction Strips for all three kits	numerator, denominator, fraction, one-half, one-
		Student Pages S85 – S93	Overhead fraction strips f 1 resealable plastic bag per student to	fourth, one-eighth, thirds, sixths, ninths, twelfths, fifths, tenths, equivalent,
		Activity Pages T885 - T886 I Have, Who Has		legal trade
10	Greatest Common	Teacher Pages T204 – T226	Centimeter cubes (10 red, 10 blue per	greatest common factor, least common multiple,
	Factor and Least Common	Student Pages S94 – S104	student pair) Colored pencils (red and blue pencils for	factor, multiple, divisible, distributive property
	Multiple	Activity Page T887 Chain Reaction	each student pair)	
11	Divide Fractions	Teacher Pages T227 – T252	Fraction kit	quotient, dividend, divisor, fraction, numerator,
		Student Pages S105 - S118		denominator, model, reciprocal, improper fraction
		Activity Page T888 Scavenger Hunt		

12	Divide Multi-Digit Numbers	Teacher Pages T253 – T275 Student Pages S119 – S133 Activity Page T889 Scavenger Hunt		quotient, dividend, divisor, remainder	
13	Add and Subtract with Decimals	Teacher Pages T276 – T300 Student Pages S134 – S148	1 sheet of colored paper for decimal foldable	decimals, addend, minuend, subtrahend, place holder, place value, tenths, hundredths, thousandths, difference,	Foldable with Decimals
		Activity Page T890 Mystery Square		sum	th Deci
14	Multiply with	Teacher Pages T301 – T326	Colored pencils – (1 red, 1 blue per	factor, product, decimal point, groups, items, array	nals
	Decimals	Student Pages S149 - S163	student pair) Calculators Foldable from Lesson 13		
		Activity Page T891 Mystery Square			
15	15 Divide with Decimals	Teacher Pages T327 – T350	Colored pencils (1 per student) Calculators Foldable from Lesson 13	dividend, divisor, quotient, decimal point	
		Student Pages S164 – S177			
		Activity Page T892 Scavenger Hunt			
16	Representing Rational	Teacher Pages T351 – T374	Colored pencils String	positive rational numbers, negative numbers,	
	Numbers	Student Pages S178 – S189	Algebra tiles	integers, opposite, elevation, above sea level,	
		Activity Page T893 Scavenger Hunt	-	below sea level, credit, debit, above zero, below zero, horizontal number line, vertical number line.	
17	17 Comparing, Ordering		Algebra tiles	inequality, less than (<), greater than (>), number	
	and Absolute Value of	Absolute S190 - S203		line, profit, loss, absolute value	
Value of Rational Numbers	Activity Page T894 Chain Reaction				

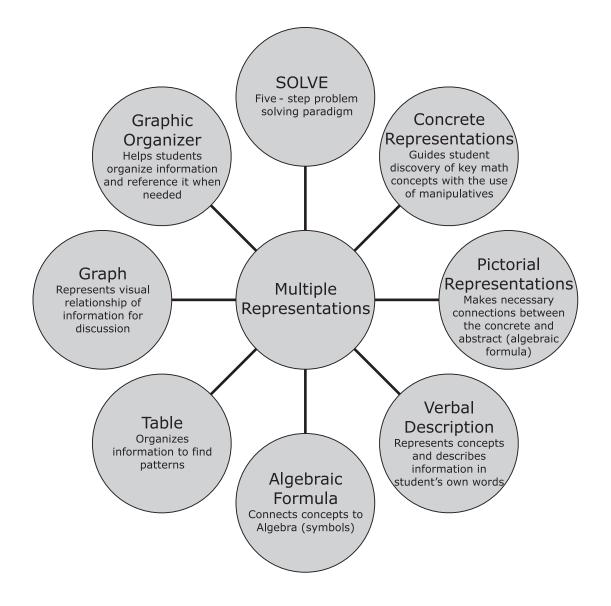
18	Plotting Points in the Coordinate Plane and on the Number Line	Teacher Pages T401 – T427 Student Pages S204 – S217 Activity Pages T895 – T898 Chain Reaction	Marker Tape Colored pencils (4 different colors) Number cards (Two Sets 1 – 10)	number line, rational numbers, horizontal number line, vertical number line, integer, reflection, coordinate plane, ordered pair, quadrant, <i>x</i> -coordinate, <i>y</i> -coordinate	
19	Solving Problems in the	Teacher Pages T428 – T451		quadrants, coordinate plane, absolute value, x-coordinates,	
	Coordinate Plane	Student Pages S218 – S232		y-coordinates	
	Flatte	Activity Pages T899 – T902 Scavenger Hunt			
		E	xpressions and Equati	ons	
20	Write and Evaluate	Teacher Pages T452 – T478	Copy Master T469 (1 per student pair) Colored paper (1 sheet per student)	evaluate, numerical expressions, exponents,	
	Numerical Expressions with	Student Pages S233 - S249		GEMDAS, verbal expressions, grouping symbols, brackets, braces,	Foldable on Expressions
	Order of Operations	Activity Page T903 Chain Reaction		parentheses, base, power, cubed, fraction bar, expression, PEMDAS	Writing
21	Write and Evaluate	Teacher Pages T479 – T504	Copy Master T495 (1 per student pair) Foldable from	variable, equation, algebraic expression, numerical expression, coefficient, constant, term, verbal expression	and E
	Algebraic Expressions with	Student Pages S247 – S259			Evaluating
	Order of Operations	Activity Page T904 Chain Reaction			ting
22	Properties of	Teacher Pages T505 – T530	Algebra tiles Overhead algebra	expressions, distributive property, associative	
	Operations and Equivalent	Student Pages S260 - S272	tiles Copy Master T525	property, commutative property, equivalent expressions, variable,	
	Expressions	Activity Page T905 Scavenger Hunt		greatest common factor, factoring, multiples, counterexample	
23	One Step Equations	Teacher Pages T531 – T555	Algebra unit tiles (6 yellow unit tiles per student pair) Cups	variable, equation, balance the equation, isolate the	
	 Add and Subtract 	Student Pages S273 – S287		variable, inverse operation	
		Activity Page T906 Chain Reaction	Overhead algebra tiles		

24	One Step Equations – Multiply and Divide	Teacher Pages T556 – T579 Student Pages S288 – S302 Activity Page T907 Scavenger Hunt	Algebra unit tiles (30 yellow unit tiles per student pair) Cups Overhead algebra tiles	variable, equation, isolate the variable, balance the equation	
25	Introduction to Inequalities	Teacher Pages T580 – T606	Centimeter cubes (2 per student pair) Copy Master T602	inequality, inverse operation(s), isolate the variable, less than, greater	
	inequalities	Student Pages S303 - S315		than, less than or equal to, greater than or equal to,	
		Activity Page T908 Mystery Square		inequality symbols (<, >, \leq , \geq), solution, number line	
26	Represent and Analyze	Teacher Pages T607 – T631	(8 yellow tiles per de student pair) in Three inch co	variable, equation, dependent variable,	
	Quantitative Relationships	Student Pages S316 - S328		independent variable, constant, discrete data, continuous data	
		Activity Pages T909 – T912 Scavenger Hunt	or cardstock (4 per student pair) Colored pencils (1 set per student pair)		
			Geometry		
27	27 Polygons in the	Teacher Pages T632 – T655		quadrants, coordinate plane, absolute value, x-coordinate, y-coordinate, area, perimeter	
	Coordinate Plane	Student Pages S329 – S342			
		Activity Pages T913 – T916 Chain Reaction			
28	Area	Teacher Pages T656 – T682	Ruler Scissors	rectangle, right triangle, area, height, base,	Geon
		Student Pages S343 – S356	Gridded index cards (1 per student) Colored pencils	perpendicular, congruent, irregular shapes, composite, compose,	netry
		Activity Pages T917 – T920 Scavenger Hunt	Colored paper for foldable (1 sheet per student) Copy Master T678	decompose, trapezoid, parallel, right angles	Geometry Foldable
29	Volume	······································	Centimeter cubes (50 cubes per pair)	volume, rectangular prism, fractional edge lengths	
		Activity Page T921 Chain Reaction			

30	Surface Area	Teacher Pages T706 – T728 Student Pages S370 – S381 Activity Page T922 Chain Reaction	Centimeter cubes (24 per student pair) Copy Master T719 Foldable from Lesson 28	surface area, rectangular prism, cube, face, net, two- dimensional
	r	[Statistics and Probabil	ity
31	Measures of Center and Variation with Dot	T729 – T753 Student Pages	Beans (24 per student pair) Calculators	mean, median, title, graph, data, scale, dot plot, data set, cluster, gap, outlier, measure of center, peak,
	Plots	S382 – S394 Activity Pages T923 – T926 Scavenger Hunt	(optional)	equally distributed
32	Box Plots and	Teacher Pages T754 – T783	Beans (21 per student pair)	box plot, Quartile 1, Quartile 3, interquartile
	Measures of Variation	Student Pages S395 – S408	Sticky notes (1 per pair cut into 6 parts so that each piece	range (IQR), median, maximum, minimum, clusters, peaks, gaps,
		Activity Pages T927 – T930 Chain Reaction		mean, scale, dot plot, data value
33	Histograms	Teacher Pages T784 – T801	Ruler (1 per student	dot plot, histogram, scale, data, intervals, frequency
		Student Pages S409 – S419		table, range
		Activity Pages T931 – T934 Scavenger Hunt		
34	Dot Plots and	Teacher Pages T802 – T826	Calculators	mean, measure of center, median, IQR (interquartile
	Measure of Variation with Mean	Student Pages S420 – S432		range), measure of variation, data set, deviation from the mean,
	Absolute Deviation	Activity Page T935 Chain Reaction		absolute value, absolute deviation, MAD (mean absolute deviation)
35	35 Summarizing Numerical	Teacher Pages T827 – T866	Calculators	statistical question, histogram, MAD(mean
	Data	Student Pages S433 – S453	absolute deviation), median, mean, clusters, statistics, data set,	
	Activity Pages T936 – T939 Scavenger Hunt	variability, variety, peak, box plot, dot plot, gaps, minimum value, maximum value, IQR (interquartile range), range, quartile, intervals, distribution		



The Key Elements to Mathematics Success Description of Teacher's Guide



SOLVE

SOLVE is a 5-step problem-solving paradigm taught in the first three lessons of *The Key Elements to Mathematics Success* and throughout the program. SOLVE is an acronym which gives students step-by-step strategies for finding the solutions to word problems. The ultimate goal of teaching SOLVE is to provide students with a problem-solving strategy that can be applied to any concept they will encounter in mathematics. The steps are as follows:

Study the Problem

Underline the question. This problem is asking me to find _____

Organize the Facts

Identify the facts. Eliminate the unnecessary facts. List the necessary facts.

Line up a Plan

Write in words what your plan of action will be. Choose an operation or operations.

Verify Your Plan with Action

Estimate your answer. Carry out your plan.

Examine Your Results

Does your answer make sense? (Compare your answer to the question.) Is your answer reasonable? (Compare your answer to the estimate.) Is your answer accurate? (Check your work.) Write your answer in a complete sentence.

Cooperative Pairs

Working in cooperative pairs is a vital part of *The Key Elements to Mathematics Success*. Cooperative learning allows students at various performance levels to work together, using a variety of learning activities, to improve their understanding. Communication about the learning process is an essential element of working in cooperative pairs. This dialogue enhances student learning and creates a sense of responsibility on the part of the students. Cooperative learning can be a catalyst in creating an atmosphere of achievement and a sense of accomplishment on the part of the students when the task is successfully completed.

Levels of Teacher Support

The lessons are carefully designed with opportunities for modeling, guided practice, and independent practice.

Modeling:

Each lesson contains "modeling boxes" which list step by step instructions on how to model each concept. Modeling steps are provided for concrete, pictorial, and procedural steps of the lesson.

Guided Practice:

Detailed instructions about how to structure guided practice are given in each lesson. Guided practice is led and closely monitored by the teacher. Students may work individually or in pairs during the guided practice.

Independent Practice:

Independent practice is provided through practice problems and homework in each lesson. Independent practice is structured to take place in the lesson following modeling and guided practice sections. Teachers can use the independent practice as a tool for informal formative assessment.

Word Problem Closure

At the end of the lesson, the SOLVE problem introduced at the beginning of the lesson is revisited. The student completes the additional steps of SOLVE, applying the lesson concept in a problem-solving situation.

Closure

Closure is a crucial part of every lesson and provides the teacher an opportunity to evaluate if the lesson objectives have been met. Teachers use the essential questions to reinforce the concept from the lesson, help organize the learning, and bring the lesson to its conclusion. A brief discussion of the essential questions will allow the teacher to informally assess student understanding of the material.

Homework

Homework is provided at the end of each lesson to give students ample opportunity to practice the lesson concept.

Quizzes

The lesson quizzes consist of 10 multiple-choice questions. These 10 questions cover the material taught in the lesson. The quizzes can also be used as homework, class work, review for a test, or as warm-ups.

Review Activities

Review activities are provided for many lessons. There are a variety of engaging activities including scavenger hunts and chain reactions. The activities are designed to provide multiple practice opportunities for the students in puzzle and game formats. The review activities incorporate the essential elements of cooperative learning and communication about the concepts.

The Key Elements to Mathematics Success – English Language Learner (ELL)

 SOLVE – A step-by-step procedure to attack word problems, dissecting the English language by identifying key words needed to solve the problem, and mapping out a plan with pictures and phrases to ultimately arrive at a well thought out answer. Steps can be written in students' native language while they are still becoming familiar with the process of SOLVE and gradually transitioning to English only. The steps of SOLVE have been modified slightly for use with ELL students. The modified steps provide additional support and involve verbal communication about the process, which is a vital link for the ELL student.

S - Underline the question. TPIAMTF (this problem is asking me to find) – **THE** ______. The students cannot just restate the question if they are made to start a sentence with *the*.

O - Circle the necessary facts. When writing out the necessary facts, be as brief as possible and teach the students abbreviations right away (\$, #, lb, cm, pkg. etc.).

L - Choose an operation and discuss a plan out loud. – +, •, \div

<u>number of nuts</u> + <u>number of bolts</u> = <u>total</u>

total • number of boxes = answer

 V - Estimate the answer out loud. Then use the set-up created in the L step to carry out the plan.

E - Choose your answer.

- **Cooperative Pairs** Working, questioning, and communicating with others regarding mathematics at all stages of learning. Activities are completed in an interactive setting, encouraging language and mathematical development. This includes the pairing of ELL students who speak the same language(s) with others who may be at varying stages of their English language development.
- **Modeling with Manipulatives** Students participate in activities leading to the discovery of on-grade-level mathematical concepts. Through this process, they develop mathematical understanding while exploring ways of expressing their discoveries in English. Manipulative use is consistent throughout the program. The appearance of each manipulative, its meaning, as well as the language used to describe the actions of these manipulatives remain the same throughout.
- Word Walls Updated through the use of KEMS lessons, new math vocabulary words (and their meaning/pictorial representation) are added for every new concept as it is discovered. The Word Wall is an interactive tool for all learners and provides an additional language resource for ELL students. Additionally an Operation Word Wall is created by each class and used for solving word problems throughout the year. As an added resource, words can be written in both English and the native language of the learner. Pictures/descriptions are also encouraged next to words wherever appropriate.
- Video Clips of Each Lesson Available for use in class at <u>www.KEMSmath.com</u>, the video clips can help overcome the significant classroom language barriers ELL students face. These video clips, though in English, show key vocabulary words as a way of familiarizing students with appropriate vocabulary used to build a concept.

SOLVE Rubric

Solve	Considerations
S Underline the question(s). (1 pt) Answered the question "What is the problem asking me to find?" (2 pt)	
Total of 3 points	
O All math facts are identified. (2 pts) Unnecessary facts are eliminated. (2 pts) Necessary facts are listed. (1 pt)	All facts get 2 points. Majority of facts get 1 point.
Total of 5 points	
L No numbers used. (1 pt) Written as a phrase or sentence. (2 pts) Explained in a logical, sequential order. (2 pts) Use of correct operation(s). (2 pts)	Logical, sequential order would include correct order of operations.
Total of 7 points	
V Make estimation. (2 pts) Number sentence matches plan from L. (2 pts) Computation is correct. (2 pts)	
Total of 6 points	
E Sentence matches S. (1 pt) Estimate was reasonable for the answer. (1 pt) Answer is correct. (1 pt) Written in a complete sentence. (1 pt)	Credit is given for writing the answer in a complete sentence, even if it is not the correct answer.
Total of 4 points	

Characters			
			_
Setting			
Action			
Fact # 1		 	
Fact # 2		 	
Other Facts		 	
Outcome (M	ain Question)		
The Problem	1:		

PROBLEM - SOLVING STORY FRAME

Total (max 10)

Points

Problem Writing Rubric

Characters	1 point: Has a character 2 points: Has characters and uses them in problem	
Scene	1 point: Has a general scene 2 points: Has a scene in which the action takes place	
Action (Facts)	1 point: Has basic needed facts (min 2) 2 points: Includes more than 2 facts 3 points: Also includes unnecessary facts	
Outcome (Question)	1 point: Has very simple question 2 points: Has more complex 1 step question 3 points: Has a multi-step question	

Problem Writing Rubric

		Points
Characters	1 point: Has a character 2 points: Has characters and uses them in problem	
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Action (Facts)	1 point: Has basic needed facts (min 2) 2 points: Includes more than 2 facts 3 points: Also includes unnecessary facts	
Outcome (Question)	1 point: Has very simple question 2 points: Has more complex 1 step question 3 points: Has a multi-step question	
	Total (max 10)	

Planning for your Key Elements to Mathematics Success Class

Materials Needed: materials needed for both the teacher and the students including items from the manipulative kit, activities to prepare for pairs on cardstock, and/or pages to copy for class

Objective: (from teacher lesson notes)

Essential Questions: (from teacher lesson notes)

Words For Word Wall: (from teacher lesson notes)

Agenda: Consider the following when planning each component of the lesson.

Activity	Time Frame	Notes/Details
Environment	N/A	 Groupings used today - seating arrangements needed? Word Wall updates for this lesson? Agenda, Objective & Essential Questions posted? Needed technology set up?
Warm-up	minutes	 What are some great questions to ask during the warm-up? How does this warm-up relate to the lesson?
Lesson	minutes	 What is the goal for today's lesson? What materials are needed? Is there an activity from the activities section of my TE that I will use to support this lesson? How does the flow of this lesson encourage student discovery of the concept being covered? What questions need to be asked to guide the discovery of today's concept? How does this lesson fit in with my district pacing guide? How will this concept be enhanced with the traditional textbook? How will I instruct partners to work? Pages being covered today Complete SOLVE Problem ASK: What is the question asking me to find? (beginning of class) What are my facts? What is my plan? What operation is needed? Estimate an answer. Work out the answer. Check over work, choose answer. What graphic organizer/foldable will be made/referenced? If time permits Will this section be used today? If so, how? How will I use the quiz for this lesson?
Closure	minutes	Essential QuestionsHomework assigned

Notes:

Planning for your Key Elements to Mathematics Success Class

Materials Needed:

Objective: Essential Questions: Words For Word Wall: Agenda:

Activity	Time Frame	Notes/Details
Environment	N/A	
Warm-up	minutes	
Lesson	minutes	
Closure	minutes	

Notes:

X