Grade
7

The Key Elements to Mathematics Success

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## Lessons

Teacher Note: When student pairs are using manipulatives to model concepts, they will need to use both partner books. Many times students need the concrete model to answer questions or bridge to the pictorial model on the following page.

|  | Lesson | Pages | Manipulatives | Word Wall Words | Foldable |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | SOLVE S and 0 | Teacher pages T1 - T19 <br> Student pages S1-S7 | Paper for foldable (3 sheets of different colors) Stapler " S " and " O " posters Index cards ("N" and "U") | S - Study the Problem <br> O - Organizer the Facts |  |
| 2 | SOLVE L | Teacher pages T20 - T39 <br> Student pages S8-S17 | Foldable from Lesson 1 Index cards (operations words) <br> "L" poster | L - Line up a Plan addition, subtraction, multiplication, division, equals, together, add, plus, and, incline, increase, deposit, sum, total, rises, grow, above, take away, difference, decline, minus, withdraw, write a check, subtract, fewer, decrease, left over, "How many?" "How much more?" below, all together, times, product, each, of, groups, items, per, double, triple, multiplied, quotient, per equal groups, cut into, divvy, split, is, same, balanced, equivalent, is equal to, divide, altogether |  |
| 3 | SOLVE V and E | $\begin{aligned} & \hline \text { Teacher pages } \\ & \text { T40 - T59 } \\ & \hline \text { Student pages } \\ & \text { S18 - S28 } \\ & \hline \end{aligned}$ | Foldable from Lesson 1 "V" and "E" posters | V - Verify Your Plan with Action <br> E - Examine Your Results |  |
| Ratios and Proportional Relationships |  |  |  |  |  |
| 4 | Unit Rates | $\begin{array}{\|l} \hline \text { Teacher pages } \\ \text { T60 - T79 } \\ \hline \text { Student pages } \\ \text { S29 - S37 } \\ \hline \text { Activity page } \\ \text { T934 Chain } \\ \text { Reaction } \\ \hline \end{array}$ | Two-color counters (12 per student pair) | ratio, unit rate, quantity, comparison, unit |  |
| 5 | Proportional Relationships | Teacher pages T80 - T101 <br> Student pages S38-S47 <br> Activity page T935 Chain Reaction | Colored pencils (1 set per student pair) | equivalent fractions, proportion, cross products, ratio, proportional relationship, unit rate, means, extremes |  |
| 6 | Identifying the Constant of Proportionality | Teacher pages <br> T102 - T122 <br> Student pages <br> S48-S56 <br> Activity pages <br> T936 - T939 <br> Scavenger Hunt | Two-color counters (15 per student pair) | constant of proportionality, unit rate, ratio, dependent variable, independent variable, coefficient |  |

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## Lessons

| 7 | Representing <br> Proportional <br> Relationships <br> with Equations | Teacher pages <br> T123 - T146 | Two-color <br> counters (12 per <br> student pair) | constant of proportionality, <br> unit rate, dependent <br> variable, independent <br> variable, coefficient |
| :--- | :--- | :--- | :--- | :--- | :--- |

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| 14 | Divide Integers | Teacher pages <br> T304 - T329 <br> Student pages <br> S151-S163 <br> Activity page <br> T960 <br> Mystery Square <br> Integer Card <br> Game T961 - <br> T962 | Overhead unit tiles <br> Red and yellow unit tiles for students (6 of each color) Foldable from Lesson 11 Playing cards (1 deck for each 4 students) | If you divvy up $\qquad$ into equal groups, what $\overline{\text { will be }}$ in each group? Splitting up $\qquad$ items into groups of $\qquad$ how many groups can you make? |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 15 | Real World Application with Rational Numbers | $\begin{array}{\|l\|} \hline \text { Teacher pages } \\ \text { T330 - T360 } \\ \hline \text { Student pages } \\ \text { S164 - S184 } \\ \hline \text { Activity pages } \\ \text { T963 - T966 } \\ \text { Scavenger Hunt } \end{array}$ | calculator | terminating decimal, repeating decimal, rational numbers |  |
|  |  |  | ssions and Eq |  |  |
| 16 | Properties of Operations with Expressions | $\begin{array}{\|l} \hline \text { Teacher pages } \\ \text { T361 - T390 } \\ \hline \text { Student pages } \\ \text { S185 - S198 } \\ \hline \text { Activity page } \\ \text { T967 } \\ \text { Chain Reaction } \end{array}$ | Overhead algebra tiles Red and yellow algebra tiles for students (8 of each tile for each student pair) Colored pencils (optional) | term, like terms, prime factorization, factor, constants, variable, expressions, zero pair, equivalent expressions |  |
| 17 | Writing Equivalent Expressions for Real World Applications | Teacher pages <br> T391 - T412 <br> Student pages <br> S199-S211 <br> Activity pages <br> T968 - T969 <br> Scavenger Hunt |  | distributive property |  |
| 18 | One-Step Equations with Integers | Teacher pages T413 - T450 Student pages S212-S230 Activity page T970 Mystery Square | Overhead unit tiles (red and yellow) Red and yellow unit tiles for students Cups | variable, equation, balance, zero pair, additive identity property |  |
| 19 | Two-Step Equations with Integers | Teacher pages T451 - T482 <br> Student pages <br> S231-S245 <br> Activity page <br> T971 Scavenger <br> Hunt | Overhead unit tiles (red and yellow) Red and yellow unit tiles for students Cups | variable, equation, balance |  |
| 20 | One and Two Step Inequalities | Teacher pages <br> T483 - T519 <br> Student pages <br> S246-S263 <br> Activity page <br> T972 <br> Mystery Square |  | inequality, inverse operation(s), isolate the variable, less than, greater than, less than or equal to, greater than or equal to, inequality symbols ( $<,>$, $\leq, \geq$ ), solution, number line |  |

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## Lessons



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Lessons


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Lessons

| 32 | Introduction to Probability | Teacher pages | Fair number cubes (1 per student pair) Colored pencils | sample space, probability, favorable outcome, possible outcome, impossible, unlikely, equally likely, likely, certain |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Student pages S420 - S433 |  |  |  |
|  |  | Activity page T1005 Scavenger Hunt |  |  |  |
| 33 | Relative Frequency | $\begin{aligned} & \text { Teacher pages } \\ & \text { T850 - T869 } \\ & \hline \end{aligned}$ | Fair number cubes (1 per student pair) Playing cards (1 deck per student pair) Centimeter cubes (6 red, 4 blue per student pair) | probability, relative frequency, trials, frequency |  |
|  |  | Student pages S434-S443 |  |  |  |
|  |  | Activity pages T1006 - T1007 Chain Reaction |  |  |  |
| 34 | Uniform and Non-Uniform Probability Models | $\begin{aligned} & \text { Teacher pages } \\ & \text { T870-T893 } \\ & \hline \end{aligned}$ | Fair number cubes (1 per student pair) Colored pencils Centimeter cubes (2 red, 2 blue, 3 green, 4 yellow per student pair) | probability model, uniform probability model, nonuniform probability model |  |
|  |  | $\begin{aligned} & \text { Student pages } \\ & \text { S444-S455 } \end{aligned}$ |  |  |  |
|  |  | Activity pages T1008 - T1011 Chain Reaction |  |  |  |
| 35 | Compound Probability | $\begin{aligned} & \text { Teacher pages } \\ & \text { T894- T923 } \\ & \hline \end{aligned}$ | Centimeter cubes Cups Fair number cubes (1 per student pair) | sample space, tree diagram, frequency table, list, simulation, compound probability |  |
|  |  | $\begin{aligned} & \text { Student pages } \\ & \text { S456-S472 } \end{aligned}$ |  |  |  |
|  |  | Activity page T1012 Chain Reaction |  |  |  |

## The Key Elements to Mathematics Success Description of Teacher's Guide




## SOLVE

SOLVE is a 5 -step problem-solving paradigm taught in the first three lessons of The Key Elements to Mathematics Success and throughout the program. SOLVE is an acronym which gives students step-by-step strategies for finding the solutions to word problems. The ultimate goal of teaching SOLVE is to provide students with a problem-solving strategy that can be applied to any concept they will encounter in mathematics. The steps are as follows:

## Study the Problem

Underline the question.
This problem is asking me to find $\qquad$ .

## Organize the Facts

Identify the facts.
Eliminate the unnecessary facts.
List the necessary facts.

## Line up a Plan

Write in words what your plan of action will be.
Choose an operation or operations.

## Verify Your Plan with Action

Estimate your answer.
Carry out your plan.

## Examine Your Results

Does your answer make sense? (Compare your answer to the question.) Is your answer reasonable? (Compare your answer to the estimate.) Is your answer accurate? (Check your work.) Write your answer in a complete sentence.

## Cooperative Pairs

Working in cooperative pairs is a vital part of The Key Elements to Mathematics Success. Cooperative learning allows students at various performance levels to work together, using a variety of learning activities, to improve their understanding. Communication about the learning process is an essential element of working in cooperative pairs. This dialogue enhances student learning and creates a sense of responsibility on the part of the students. Cooperative learning can be a catalyst in creating an atmosphere of achievement and a sense of accomplishment on the part of the students when the task is successfully completed.

## Levels of Teacher Support

The lessons are carefully designed with opportunities for modeling, guided practice, and independent practice.

## Modeling:

Each lesson contains "modeling boxes" which list step by step instructions on how to model each concept. Modeling steps are provided for concrete, pictorial, and procedural steps of the lesson.

## Guided Practice:

Detailed instructions about how to structure guided practice are given in each lesson. Guided practice is led and closely monitored by the teacher. Students may work individually or in pairs during the guided practice.

## Independent Practice:

Independent practice is provided through practice problems and homework in each lesson. Independent practice is structured to take place in the lesson following modeling and guided practice sections. Teachers can use the independent practice as a tool for informal formative assessment.

## Word Problem Closure

At the end of the lesson, the SOLVE problem introduced at the beginning of the lesson is revisited. The student completes the additional steps of SOLVE, applying the lesson concept in a problem-solving situation.

## Closure

Closure is a crucial part of every lesson and provides the teacher an opportunity to evaluate if the lesson objectives have been met. Teachers use the essential questions to reinforce the concept from the lesson, help organize the learning, and bring the lesson to its conclusion. A brief discussion of the essential questions will allow the teacher to informally assess student understanding of the material.

## Homework

Homework is provided at the end of each lesson to give students ample opportunity to practice the lesson concept.

## Quizzes

The lesson quizzes consist of 10 multiple-choice questions. These 10 questions cover the material taught in the lesson. The quizzes can also be used as homework, class work, review for a test, or as warm-ups.

## Review Activities

Review activities are provided for many lessons. There are a variety of engaging activities including scavenger hunts and chain reactions. The activities are designed to provide multiple practice opportunities for the students in puzzle and game formats. The review activities incorporate the essential elements of cooperative learning and communication about the concepts.

## The Key Elements to Mathematics Success - English Language Learner (ELL)

- SOLVE - A step-by-step procedure to attack word problems, dissecting the English language by identifying key words needed to solve the problem, and mapping out a plan with pictures and phrases to ultimately arrive at a well thought out answer. Steps can be written in students' native language while they are still becoming familiar with the process of SOLVE and gradually transitioning to English only. The steps of SOLVE have been modified slightly for use with ELL students. The modified steps provide additional support and involve verbal communication about the process, which is a vital link for the ELL student.
S - Underline the question. TPIAMTF (this problem is asking me to find) - THE $\qquad$ . The students cannot just restate the question if they are made to start a sentence with the. O - Circle the necessary facts. When writing out the necessary facts, be as brief as possible and teach the students abbreviations right away (\$, \#, lb, cm, pkg. etc.).
L - Choose an operation and discuss a plan out loud. $-+, \bullet, \div$ number of nuts + number of bolts $=$ total
total - number of boxes $=$ answer
V - Estimate the answer out loud. Then use the set-up created in the L step to carry out the plan.
E-Choose your answer.
- Cooperative Pairs - Working, questioning, and communicating with others regarding mathematics at all stages of learning. Activities are completed in an interactive setting, encouraging language and mathematical development. This includes the pairing of ELL students who speak the same language(s) with others who may be at varying stages of their English language development.
- Modeling with Manipulatives - Students participate in activities leading to the discovery of on-grade-level mathematical concepts. Through this process, they develop mathematical understanding while exploring ways of expressing their discoveries in English. Manipulative use is consistent throughout the program. The appearance of each manipulative, its meaning, as well as the language used to describe the actions of these manipulatives remain the same throughout.
- Word Walls - Updated through the use of KEMS lessons, new math vocabulary words (and their meaning/pictorial representation) are added for every new concept as it is discovered. The Word Wall is an interactive tool for all learners and provides an additional language resource for ELL students. Additionally an Operation Word Wall is created by each class and used for solving word problems throughout the year. As an added resource, words can be written in both English and the native language of the learner. Pictures/descriptions are also encouraged next to words wherever appropriate.
- Video Clips of Each Lesson - Available for use in class at www.KEMSmath.com, the video clips can help overcome the significant classroom language barriers ELL students face. These video clips, though in English, show key vocabulary words as a way of familiarizing students with appropriate vocabulary used to build a concept.


## SOLVE Rubric

| Solve | Considerations |
| :---: | :---: |
| S <br> Underline the question(s). (1 pt) Answered the question "What is the problem asking me to find?" (2 pt) <br> Total of 3 points |  |
| 0 <br> All math facts are identified. (2 pts) Unnecessary facts are eliminated. (2 pts) Necessary facts are listed. (1 pt) <br> Total of 5 points | All facts get 2 points. Majority of facts get 1 point. |
| L <br> No numbers used. (1 pt) <br> Written as a phrase or sentence. <br> (2 pts) <br> Explained in a logical, sequential order. <br> (2 pts) <br> Use of correct operation(s). (2 pts) <br> Total of 7 points | Logical, sequential order would include correct order of operations. |
| V <br> Make estimation. (2 pts) <br> Number sentence matches plan from L. (2 pts) Computation is correct. (2 pts) <br> Total of 6 points |  |
| E <br> Sentence matches S. (1 pt) <br> Estimate was reasonable for the <br> answer. (1 pt) <br> Answer is correct. (1 pt) <br> Written in a complete sentence. (1 pt) <br> Total of 4 points | Credit is given for writing the answer in a complete sentence, even if it is not the correct answer. |

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PROBLEM - SOLVING STORY FRAME

Characters $\qquad$
$\qquad$
Setting $\qquad$
Action
Fact \# 1
Fact \# 2
Other Facts $\qquad$
$\qquad$
Outcome (Main Question)

The Problem:
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Problem Writing Rubric

Points

| Characters | 1 point: Has a character <br> 2 points: Has characters and uses them in problem |
| :---: | :---: |
| Scene | 1 point: Has a general scene <br> 2 points: Has a scene in which the action takes place |
| Action (Facts) | 1 point: Has basic needed facts ( $\min 2$ ) <br> 2 points: Includes more than 2 facts <br> 3 points: Also includes unnecessary facts |
| Outcome (Question) | 1 point: Has very simple question <br> 2 points: Has more complex 1 step question <br> 3 points: Has a multi-step question |

Total (max 10)

## Problem Writing Rubric

|  |  |
| :---: | :---: |
| Characters | 1 point: Has a character <br> 2 points: Has characters and uses them in problem |
| Scene | 1 point: Has a general scene <br> 2 points: Has a scene in which the action takes place |
| Action (Facts) | 1 point: Has basic needed facts ( $\min 2$ ) <br> 2 points: Includes more than 2 facts <br> 3 points: Also includes unnecessary facts |
| Outcome (Question) | 1 point: Has very simple question <br> 2 points: Has more complex 1 step question <br> 3 points: Has a multi-step question |
|  | Total (max 10) |

## Planning for your Key Elements to Mathematics Success Class

Materials Needed: materials needed for both the teacher and the students including items from the manipulative kit, activities to prepare for pairs on cardstock, and/or pages to copy for class
Objective: (from teacher lesson notes)
Essential Questions: (from teacher lesson notes)
Word Wall Words: (from teacher lesson notes)
Agenda: Consider the following when planning each component of the lesson.

| Activity | Time Frame | Notes/Details |
| :---: | :---: | :---: |
| Environment | N/A | - Groupings used today - seating arrangements needed? <br> - Word Wall updates for this lesson? <br> - Agenda, Objective \& Essential Questions posted? <br> - Needed technology set up? |
| Warm-up | minutes | - What are some great questions to ask during the warm-up? <br> - How does this warm-up relate to the lesson? |
| Lesson | $\overline{\text { minutes }}$ | - What is the goal for today's lesson? <br> - What materials are needed? <br> - Is there an activity from the activities section of my <br> TE that I will use to support this lesson? <br> - How does the flow of this lesson encourage student discovery of the concept being covered? What questions need to be asked to guide the discovery of today's concept? <br> - How does this lesson fit in with my district pacing guide? <br> - How will this concept be enhanced with the traditional textbook? <br> - How will I instruct partners to work? <br> - Pages being covered today... <br> - Complete SOLVE Problem <br> ASK: What is the question asking me to find? (beginning of class) <br> What are my facts? <br> What is my plan? What operation is needed? <br> Estimate an answer. <br> Work out the answer. <br> Check over work, choose answer. <br> - What graphic organizer/foldable will be made/referenced? <br> - If time permits... <br> - Will this section be used today? <br> - If so, how? <br> - How will I use the quiz for this lesson? |
| Closure | $\overline{\text { minutes }}$ | - Essential Questions <br> - Homework assigned |

## Notes:

## Planning for your Key Elements to Mathematics Success Class

## Materials Needed:

Objective:
Essential Questions:
Word Wall Words:
Agenda:

| Activity | Time <br> Frame |  |
| :---: | :---: | :---: |
| Environment | N/A |  |
| Warm-up | $\overline{\text { minutes }}$ |  |
| Lesson | $\overline{\text { minutes }}$ |  |
| Closure |  |  |

## Notes:

